A revised mechanistic model for sodium insertion in hard carbons

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Abstract

Hard carbons have shown considerable promise as anodes for emerging sodium-ion battery technologies. Current understanding of sodium-storage behaviour in hard carbons attributes capacity to filling of graphitic interlayers and pores, and adsorption at defects, although there is still considerable debate regarding the voltages at which these mechanisms occur. Here, *ex situ* ²³Na solid-state NMR and total scattering studies on a systematically tuned series of hard carbons revealed the formation of increasingly metallic sodium clusters in direct correlation to the growing pore size, occurring only in samples which exhibited a low voltage plateau. Combining experimental results with DFT calculations, we propose a revised mechanistic model in which sodium ions store first simultaneously and continuously at defects, within interlayers and on pore surfaces. Once these higher energy binding sites are filled, pore filling occurs during the plateau region, where the densely confined sodium takes on a greater degree of metallicity.

1. Introduction

As the global energy demand increases, the development of effective and sustainable energy storage systems is becoming critically important. Whilst lithium-ion batteries (LIBs) are an established technology,¹ the uneven global distribution and limited supply of lithium reserves greatly restricts their use for large-scale energy storage applications. Sodium-ion batteries (NIBs) are considered a natural successor to LIBs because of their similar chemical and electrochemical properties,² offering a more sustainable and lower cost alternative. However, one significant limitation in the progress of NIB technology has been the development of suitable anode materials.³ Graphite anodes are widely used in LIBs, forming the stage one graphite intercalation compound (GIC) LiC₆ with a reversible capacity of 372 mAh g^{-1.4} On the other hand, in conventional electrolytes sodium ions cannot intercalate into graphite to any great extent (NaC₆₄),⁵ and therefore graphite is unsuitable for NIB applications.

Instead, since the first report by Stevens and Dahn in 2000,⁶ much research has been conducted into non-graphitic hard carbons as NIB anodes, and these materials have exhibited promising reversible capacities around 300 mAh g⁻¹.^{3, 4, 7, 8} Hard carbons are composed of randomly-oriented, curved and defective graphene nanosheets, turbostratically stacked with large interlayer distances,^{9, 10} providing sodium storage capacity at defects and sheet edges, within pores, and between expanded graphene layers. For hard carbons, the characteristic charge-discharge profiles typically exhibit a sloping region between 1.0 and 0.1 V, and a plateau below 0.1 V. In previous studies, these two regions have generally been attributed to distinct sodium storage mechanisms. The early model proposed by Stevens and Dahn based on small and wide angle X-ray scattering (SAXS, WAXS) analysis assigned sodium intercalation to the sloping voltage region, and micropore filling to the low voltage plateau.^{11, 12} This model was later supported by operando nuclear magnetic resonance (NMR) spectroscopy and X-ray scattering analysis.^{13, 14, 15} In contrast, an alternative model was proposed consisting of surface and defect adsorption in the sloping region followed by interlayer intercalation in the low voltage plateau, with sodium plating occurring close to 0 V;¹⁶ subsequent reports have suggested different combinations of these various Na storage processes.^{17, 18, 19, 20, 21, 22} However, several of these studies dismiss pore filling based on the low pore volumes observed using gas adsorption techniques.^{21, 22} The development of *operando* and *in situ* measurements in techniques such as SAXS, WAXS, X-ray diffraction (XRD)^{11, 12, 19} and NMR spectroscopy¹³ has enabled these studies, although there is still considerable debate regarding the sodium storage mechanisms at different voltages. These investigations have studied a range of different carbons and, therefore, the conflicting explanations are hardly surprising, given the dependence of structural morphology, porosity and surface area on the precursor material and synthesis method. Generally, carbons were obtained from simple sugars, natural biomass or polymer precursors, and converted either by direct pyrolysis, microwave irradiation, hydrothermal carbonisation or a combination of these processes.^{23, 24, 25, 26, 27, 28, 29, 30, 31, 32} Hydrothermal carbons, in particular, are well-suited for energy storage applications since the spherical morphology obtained after treatment enables uniform charge distribution across particle surfaces and a better packing density in the electrode, whilst the low surface area-to-volume ratio can minimise the extent of the solid electrolyte interphase (SEI) formed in the first cycle.^{23, 33}

In this work, a series of hard carbons was prepared by hydrothermal treatment of glucose followed by high temperature pyrolysis; by altering the temperature, the porosity, number of defects, and graphitic structure could be systematically tuned. A correlation between the microstructure and sodium storage behaviour was established with *ex situ*²³Na NMR spectroscopy, X-ray and neutron scattering, and supported with density functional theory (DFT) calculations. In particular, the NMR measurements demonstrated the increasingly metallic nature of the stored sodium with increasing pore size. This quasimetallic environment was only present in the carbons that exhibited a low voltage plateau, supporting the mechanistic assignment of pore filling during this region. However, while higher pyrolysis temperatures increase pore capacity, diffusion pathways within graphite interlayers and across defects are reduced, rendering some pores inaccessible and limiting sodium storage in the sloping region; optimising the performance of hard carbons is therefore a balance between maintaining an expanded interlayer distance, the number of defects, and open diffusion pathways, whilst also maximising the size of accessible pores.

2. Results

Synthesis and structural characterisation of glucose-derived hard carbons

A series of hard carbons was prepared by hydrothermal carbonisation $(HTC)^{34}$ of glucose (denoted GHTC), followed by pyrolysis at different temperatures (1000 °C, 1300 °C, 1500 °C, 1700 °C, 1900 °C) to remove heteroatom defects, introduce conductivity, and tune porosity, yielding the five samples G1000, G1300, G1500, G1700 and G1900. The resulting carbons retained their spherical morphology after high temperature carbonisation (Figure 1a and b) whilst the pyrolysis temperature had little effect on particle size with all samples showing agglomerated carbon spheres in the range 200 nm-5 µm (Figure S1). The variation in electrochemical behaviour can therefore be fully attributed to the materials' structural and compositional differences.



Figure 1. SEM images of a) GHTC and b) G1500; scale bars 5 µm; core level c) C1s and d) O1s spectra for GHTC; core level e) C1s and f) O1s spectra for G1500.

Subsequent high temperature heat treatment successfully removed polar surface groups and heteroatom defects, as confirmed by X-ray photoelectron spectroscopy (XPS) (Figure 1c-f, S2). In the high resolution O1s spectrum of GHTC, peaks at 533.2 eV and 532.0 eV can be assigned to C-O and C=O bonds respectively (Figure 1d), corresponding to deconvoluted peaks at 287.3 eV and 289.2 eV in the C1s core-level spectrum (Figure 1c).³⁵ After pyrolysis, these C-O and C=O peaks are significantly

weaker indicating a substantial reduction in oxygen functionalities (Figure 1e and f). Analysis of the higher resolution data indicates a composition of 18.1 at% O and 81.9 at% C after HTC; this ratio is significantly decreased after high temperature carbonisation, with a decreasing amount of O with increasing temperature (5.9-1.3 at%, Table 1).

The microstructure of these materials was tuned by varying the pyrolysis temperature between 1000 and 1900 °C. TEM images reveal structures typical of hard carbons composed of mostly disordered domains with some regions of graphitic stacking (Figure 2a-e). At 1000 °C, amorphous domains dominate, whereas in the samples treated at 1700 and 1900 °C, larger areas of graphitic stacking become apparent, since greater order is introduced with increasing carbonisation temperature. These results are consistent with the rearrangement of disordered crosslinked carbon regions into a coherent sp² network, alongside the loss of oxygen functionalities.



Figure 2. TEM images of a) G1000, b) G1300, c) G1500, d) G1700, and e) G1900; scale bars 5 nm; f) Raman spectra of G1000, G1300, G1500, G1700 and G1900, $\lambda_{exc} = 633$ nm.

Further evidence for the evolution of structural ordering with temperature was obtained by Raman spectroscopy (Figure 2f). Hard carbons generally exhibit broad signals around 1350 and 1580 cm⁻¹ (D- and G-band, respectively), related to in-plane sp² C-bond breathing and stretching modes, and often no 2D signal at ~2700 cm⁻¹, which provides information regarding graphitic layer stacking and

coherence.^{36, 37} The Raman spectrum of G1000 is characteristic of hard carbon, with very broad D and G bands and an extremely weak 2D signal; with increasing pyrolysis temperature, the peaks narrow and sharpen, and the intensity ratio I_D/I_G increases (Figure 2f). This I_D/I_G trend is consistent with the loss of residual oxygen functionalities and increasing in-plane ordering ($L_a = 0.8$ nm in G1000 to $L_a = 1.2$ nm in G1900, Table 1),³⁸ and the sharpening of signals implies conversion of rings with order other than six into aromatic rings.³⁷ Furthermore, a 2D signal appears in the samples pyrolysed at 1700 °C and above, implying that some graphitic layer coherence is developing, consistent with the observations made by TEM.

The development of structural ordering is also observed in the neutron total scattering (Figure 3a) and SAXS/WAXS (Figure S3) patterns, where both the interlayer distance (d_{002}) and the in-plane distance (d_{100}) approach the values for graphite with increasing temperature (Figure 5b and S4). Furthermore, an increase in the stack thickness and in-plane crystallite size (Figure 3e and f) was calculated, with stacks of 2-3 graphene layers with 1.5-2 nm wide basal planes for the lower temperature G1000-G1500 samples, and stacks of up to 10-15 graphene layers with 4 nm wide basal planes for the G1900 sample. These results are consistent with the qualitative observations made by TEM and the trend in L_a (Table 1) calculated from Raman data, although the results from Raman may be considered an underestimate due to the dominant effects of small crystallites.³⁷ In the pair distribution functions (PDF) (Figure 3b) and difference PDFs (Figure 3c), the signal at ~1.4 Å (d₁, Figure S4a) indicates that the carbon material after HTC contains mostly sp²-hybridised carbon, but with a substantial amount of sp³-hybridised carbon, observed by the shoulder on the peak, around 1.5 Å. These sp³ carbons disappear after heating to 1000 °C, indicated by the negative peak in the difference PDF at ~1.6 Å (Figure 3c), consistent with XPS results (Figure 1c and e). The appearance of the signal at 2.8 Å (d₃, Figure S4a), characteristic of the C_1 - C_4 distance in a benzene ring, confirms the growth of aromatic domains within the material. The largest change in PDF is observed between GHTC and G1000, indicating that the initial graphitisation takes place at low temperature as expected (Figure 3c). The next significant structural change occurs from G1500 to G1700 where the development of longer-range order is evident from the increased signal at higher distances (Figure 3c). This observation also corresponds to the trends in graphitic ordering

and domain size obtained from analysis of the 002 and 100 peaks (Figure 3e, f and S4), where the largest structural difference occurs between these two pyrolysis temperatures; similarly, in the Raman spectra, the 2D band only appears above 1700 °C. These results suggest that below 1500 °C, nucleation of graphitic regions is the predominant reaction occurring within the material, without large changes to the domain size. Above 1500 °C, growth of the graphitic domains and ordering of the stacked planes are the dominant processes, although in some regions rearrangement is constrained, reflected in the double peak model required to fit the 002 peak in the high temperature data (Figure S3).

The pore diameters were also calculated from the Guinier-Porod region^{11, 39} in the small angle neutron scattering (SANS) (Figure 3a) and SAXS (Figure S3 and S4) data and were found to be very similar in size to the corresponding basal planes; dimensions of 1-2 nm for G1000-G1500 and up to a maximum size of 5 nm for G1900 (Figure 5b) were observed, suggesting that the pore size is dependent on the lateral size of the graphene basal plane. The lack of any structure factor peaks suggests that the pores are relatively dilute, as there would otherwise be pore-pore correlation peaks in the SAXS/SANS region. The relative pore volumes, obtained using the Guinier-Porod model¹¹ (equations S1-3), for the G1000-G1500 materials remain similar, suggesting only limited pore creation within this temperature range (Figure 3d). Above 1500 °C, a significant change in pore volume was observed, increasing by a factor of three between G1500 and G1900. In contrast, the total pore volume determined from N2 adsorption significantly decreased, with a 90% loss between G1000 and G1300 (Figure 3d and S5, Table S1). Correspondingly, the glucose-derived carbon pyrolysed at 1000 °C has the highest specific surface area of 382 m² g⁻¹; at temperatures above 1000 °C, the surface area decreases dramatically to $\sim 10 \text{ m}^2 \text{ g}^{-1}$ (Table 1). The pore volume and surface area values calculated from the CO_2 adsorption isotherms are generally higher than those from N₂ measurements, since CO₂ can probe smaller pores, and decrease more gradually with elevated temperatures (Figure 3d and S5, Table 1), whilst the pore size distributions from both measurements indicate that the materials are mostly micro- and mesoporous (Figure S5). The discrepancy with the trends observed from SAXS/SANS analysis suggests that although porosity is developing as the carbons are heated, above 1000 °C the larger pores and subsequently the micropores close off during pyrolysis, becoming inaccessible to gas molecules, but remain observable by X-ray and neutron scattering.



Figure 3. a) Structure factor (S(Q)), and b) PDF (D(r)) of the carbons before and after high temperature treatment. The SANS region was removed before Fourier transform to the PDF to remove pore-pore correlations; c) difference PDF between each temperature with the PDF of GHTC and G1900 included for reference; d) relative change in the pore volume probed by N_2 and CO_2 gas adsorption and the intensity of the Guinier plateau in the small angle region weighted by pore volume; e) stack thickness, and f) domain size of the graphitic regions derived from the width of the 002 and 100 peaks. Additional SAXS data and example model fits are shown in Figure S3.

Overall, the characterisation indicates that although the particle morphology is maintained after carbonisation, the structures of the glucose-derived carbons are highly tuneable by altering the pyrolysis temperature, with greater ordering arising from fewer defects, increasing aromaticity, decreasing interlayer spacing, and larger crystallite size. Pore size and surface area are also highly dependent on the temperature of carbonisation with the development of larger, closed pores above 1500 °C.

Electrochemical performance in Na-ion half cells

In order to investigate the structural influences on the performance and storage mechanism in NIBs, electrochemical testing of the materials was carried out in half cells using sodium metal as the counter electrode, in the voltage window 0-2.5 V. During galvanostatic cycling at 30 mA g^{-1} , the carbons exhibit a range of reversible capacities (96-293 mAh g^{-1}) and first cycle Coulombic efficiencies (FCCE) (39-96 %) (Figure 5a and Table S1), with the highest performing G1500 comparing reasonably with

other previously reported carbonaceous materials.² The discharge curves of the samples show varying profiles, from which insight into the sodium storage mechanism may be gained; G1300 and G1500 derive their capacity from both the slope and plateau regions (Figure 5b and Table S1), whereas G1700 and G1900 both show mainly plateau capacity. Conversely, the capacity of G1000 is exclusively in the sloping region, and is highly irreversible in the first cycle, consistent with having the highest surface area available for SEI formation, and many defect sites and oxygen functionalities where sodium may remain trapped. A corresponding reduction peak is observed in the cyclic voltammogram between 0.7 and 0 V in the first cycle (Figure S6), and similar smaller irreversible peaks appear in the other samples, reflecting the irreversible capacity processes occurring in the first cycle.

Ex situ ²³Na NMR of the sodiated carbons

Analysis of the *ex situ*²³Na magic-angle spinning (MAS) ssNMR spectra of the fully sodiated materials provides insight into how the sodium storage environments vary according to the carbon structure (Figure 4a). A sharp peak is observed at around 0 ppm for all of the carbons, which is attributed to diamagnetic sodium in the residual electrolyte salt and SEI layer.¹³ In the spectrum of G1300, a broad peak is observed centred at about 750 ppm (Figure 4b). This shift falls well outside the range of diamagnetic sodium compounds, indicating that this species is exhibiting a Knight shift caused by the presence of conduction electrons (metallic sodium exhibits a peak at 1135 ppm).⁴⁰ In the lowest temperature-treated material, this quasi-metallic peak is non-existent, implying that sodium stored in the sloping region is mainly ionic in nature, consistent with sodium adsorbed at defects, interlayers or pore surfaces.¹³ With higher heat treatment, the quasi-metallic peak grows in intensity and shifts to higher frequency, closer to that of sodium metal (Figure 4b). In G1900, the presence of metallic sodium is clear from the strong peak observed at 1135 ppm. Interestingly, in these samples which were discharged to 5 mV, metallic sodium was observed before reaching 0 V, contrary to previous reports.^{15,} ^{16, 19, 21} The growing metallic character of the sodium corresponds to the increasing pore size with temperature and is consistent with the growth of sodium clusters within the pores (Figure 4b). Here, beyond the first adsorbed monolayer, sodium ions must necessarily be reduced to minimise charge repulsion which would otherwise prevent confinement of many sodium ions within one space.

Therefore, the larger the pore and subsequently the cluster, the greater the metallic character of the sodium environment, corresponding to the progressive shift of the sodium peak to higher frequencies with increased temperatures.



Figure 4. a) Ex situ ²³Na MAS NMR of G1000-G1900 after discharging to 5 mV, b) relationship between the pore diameter, quasi-metallic Na peak shift and sample pyrolysis temperature.

Sodium storage mechanisms in hard carbons

Combining the materials analysis and electrochemical characterisation allows us to correlate the hard carbon structure with the different sodium storage processes occurring during cell discharge. With increasing carbonisation temperature, the pore size increases, whilst the O/C ratio, degree of defects and graphitic interlayer spacing all decrease (Figure 5b); concurrently, in their voltage profiles, the capacity contribution from the sloping region generally decreases, whilst the plateau region increases, before dropping off at higher temperatures. In our revised mechanistic model, we propose that during the initial stages of sodiation, between 2.5 and 0.1 V, sodium storage occurs simultaneously at defects,

within interlayer galleries and at pore surfaces. Once these sites are filled, residual pore filling takes place, below 0.1 V, until full sodiation is achieved.

In the sloping region, the changing voltage profile is a result of a combination of energetically different processes, as well as the continuous structural distortion arising from the interlayer expansion which accompanies the insertion of sodium ions.^{41, 42} While sodium diffusion within curved pores is rapid compared to inside graphitic interlayer galleries⁴³ and across heteroatom defects,⁴⁴ the ions are less strongly bound at these pore surfaces.⁴³ Therefore, interlayer intercalation and filling of defect sites occur preferentially to pore filling. DFT calculations of sodium binding in bilayer and monolayer graphitic models (Figure S9) indicate that different defect types influence the energetics of sodium storage differently, both at the defect site and at sites adjoining the defect. These simulations show that oxygen defects in the graphitic bilayer and on the surface lead to stronger sodium adsorption energies, especially at low sodium loading. Furthermore, the effect of oxygen-containing defects is not localised and can also improve the sodium storage at sites away from the defects, although at higher sodium concentrations, or higher specific capacities, the effect is reduced. Similarly, sodium intercalation in the graphitic bilayer model is mainly affected by the presence of the 2O_C bilayer defect (Figure S8) at x_{Na} <3. At higher Na concentrations, the added Na start to fill the non-defective sites, so the calculated binding energies approach those of the non-defective graphitic bilayer (Figure S9). Comparing all the simulated systems (Figure S9), at low x_{Na} (corresponding to low specific capacity), sodium storage at surface defects dominates, whereas as soon as the defect sites become saturated, sodium intercalation in expanded graphitic bilayers becomes energetically favourable too. Some studies have previously attributed the sloping region capacity to defect adsorption only;^{16, 18, 21} with this series of materials, considering the scenario in which each sodium binds to one oxygen-containing defect, the maximum theoretical capacity derived from defect adsorption (Table S2) can only account for 48-79% of the total sloping capacity. Therefore, in combination with these and previous simulated results,^{42, 43, 44} both sodium adsorption and intercalation in defective and turbostratic carbon regions contribute to the experimentally observed sloping voltage profiles. G1000, which has the highest concentration of oxygen-containing defects (5.9 at%) and the widest interlayer spacing (3.9 Å), exhibits the largest

sloping capacity; the sloping capacity decreases with higher carbonisation temperatures, corresponding to the decrease in interlayer spacing and number of defects (Figure 5b). In addition, the onset voltage of the sloping region for the two high temperature materials is also lower (~ 0.5 V vs. ~ 1 V in G1000-G1500), indicative of the absence of defects as higher energy sodium binding sites (Figure 5a).



Figure 5. a) Galvanostatic charge/discharge profiles for G1000-G1900 in the first and second cycles; b) summary of the structural evolution of the hard carbons and capacity contributions with increasing pyrolysis temperature (lines are a guide for the eye only); c) schematic illustration of the proposed sodium storage mechanism; stack thickness and plane size are not to scale, and defects and curvature are not explicitly shown.

Once all the available interlayer and defect sites are occupied, we hypothesise that residual filling of the pores takes place until the electrode is fully sodiated. Insertion of sodium into pores results in negligible structural distortion so the binding site energy remains almost constant; in addition, the sodium binding energy is weak,⁴³ and pore filling therefore corresponds to the low voltage plateau below 0.1 V. The NMR results support this mechanistic assertion, where the quasi-metallic environment was only observed in the carbons that exhibited plateau capacity (Figure 4). However, the plateau capacity does not monotonically increase with pore size but reaches a maximum at 1500 °C (Figure

5b). While the pore size continues to increase, the decrease in expanded graphitic stacks results in fewer diffusion pathways reaching the pores, and consequently some pores become inaccessible for sodium storage, corresponding to a smaller plateau capacity. The decrease in diffusion pathways also contributes to the diminishing performance at higher current densities, where G1700 and G1900 exhibit the poorest electrochemical performance across the range of current densities (Figure S7).

To summarise, G1000 has the highest concentration of defects and the widest interlayer spacing available for sodium storage, but pore filling is minimal due to the small diameter of the pores, resulting in a discharge profile entirely composed of sloping capacity (Figure 5c bottom panel). At intermediate pyrolysis temperatures, the number of oxygen defects decreases, and the interlayer spacing narrows slightly, but storage capacity from pores increases with the larger pore size; a decreasing slope capacity and a greater contribution from the plateau region are therefore observed in G1300 and G1500 (Figure 5c middle panel). In G1700 and G1900, the number of defects is very low, and there are even fewer expanded graphitic domains accessible for sodium intercalation as the interlayer spacing narrows; therefore, the capacity in the sloping region decreases significantly. Furthermore, whilst the pore size continues to increase, diffusion pathways are closed off, and consequently some pores become inaccessible for sodium storage, corresponding to a smaller plateau capacity (Figure 5c top panel).

Overall, the correlation between pore size, quasi-metallic sodium and plateau capacity provides strong evidence that pore filling occurs in the plateau region, and our revised model is in good agreement with the original proposed by Stevens and Dahn,¹¹ and several others.^{13, 15, 18, 19, 29} However, we believe that each of these models alone insufficiently describes the processes occurring during the slope region, and that, based on the structural trends in these materials, it is reasonable to hypothesise that the slope capacity may be assigned to simultaneous and continuous processes of defect adsorption, interlayer intercalation, and adsorption on pore surfaces. Furthermore, the plateau capacity derived from pore filling is not independent of the structural characteristics associated with sloping capacity; as the graphitic interlayer spacings decrease, there are fewer diffusion pathways allowing sodium ions to reach the pores, rendering them inaccessible for sodium storage. The highest performance of the carbon pyrolysed at 1500 °C therefore results from the optimal combination of intermediate pore size with

wide interlayer spacings which provide storage to sodium ions and diffusion channels into pores, as well as defects which serve as additional adsorption sites.

Sample	C at%	O at%	C/O	La (nm) ³⁶	$S_{BET}(N_2)^a (m^2 g^{-1})$	$S_{DR}(CO_2)^b (m^2 g^{-1})$
GHTC	81.9	18.1	4.5	-	-	-
G1000	94.1	5.9	15.9	0.8	382	786
G1300	96.0	4.0	24.3	1.0	10	128
G1500	96.7	3.3	29.0	1.0	11	74
G1700	97.7	2.3	43.9	1.2	7	15
G1900	98.7	1.3	74.9	1.2	7	18

Table 1. XPS atomic compositions, Raman in-plane lattice size, and specific surface areas calculated from N_2 and CO_2 adsorption isotherms of the hard carbon materials.

^{*a}</sup><i>Calculated using the Brunauer-Emmett-Teller (BET) method.* ^{*b*}*Calculated using the Dubinin-Radushkevich method.*</sup>

3. Discussion

A series of hard carbons was prepared by hydrothermal carbonisation of glucose followed by high temperature treatment and the development of the carbon structure with pyrolysis was extensively characterised. A relationship between defect concentration, interlayer spacing, porosity and electrochemical behaviour was established, where the sloping region capacity is attributed to simultaneous and continuous sodium storage at defects, within interlayers and on pore surfaces, across a range of different binding energies. Subsequently, pore filling occurs during the low voltage plateau region, becoming increasingly metallic with increasing pore size, as demonstrated by *ex situ*²³Na NMR. However, despite the higher porosity, the closing of diffusion pathways at high temperature results in an overall lower capacity, as these pores become inaccessible to sodium. At the same time, the high surface area of the G1000 carbon resulted in a large irreversible capacity, and the material carbonised at 1500 °C exhibited the highest capacity, confirming that a balance between these different structural factors is crucial to improved electrochemical performance. These findings provide insight into the future design and development of hard carbons for NIBs, to achieve materials with optimised interlayer spacings, open diffusion channels, defects, and porosity.

4. Methods

Materials synthesis. Hard carbons were prepared by hydrothermal carbonisation (HTC) of glucose. In a typical batch, 10 g glucose (D-(+)-glucose, \geq 99.5%, Sigma-Aldrich) was dissolved in 90 mL deionised water. The solution was placed in a sealed 200 mL autoclave reactor vessel and heated at 230 °C for 12 hours. After reaction, the resulting solid (GHTC) was separated from the supernatant and dried under vacuum at 80 °C overnight, and then further carbonised at 1000, 1300, 1500, 1700 or 1900 °C for 2 hours under a nitrogen atmosphere, to yield the five materials G1000, G1300, G1500, G1700, and G1900 (overall yield 23-26%).

Materials characterisation. Scanning electron microscopy (SEM) was carried out using a FEI Inspect-F SEM at 10 kV. The carbon samples were mounted onto stainless steel stubs with double-sided carbon tape. X-ray photoelectron spectroscopy (XPS) data were recorded using a ThermoFisher Nexsa X-ray spectrometer equipped with an Al K α monochromated X-ray source. Survey scans were acquired using 200 eV pass energy, 1 eV step size and 200 ms (10 ms \times 20 scans) dwell times. All high-resolution spectra were acquired using 50 eV pass energy, 0.1 eV step size and 1 s (50 ms \times 20 scans) dwell times. Samples were prepared by pressing the sample onto double-sided carbon tape. Pressure during measurement acquisition was $\leq 1 \times 10^{-9}$ mbar. Atomic compositions were calculated from averaged spectra obtained from 3 areas per sample. Transmission electron microscopy (TEM) was carried out using a JEOL 2100Plus TEM at 200 kV operating voltage. Samples were prepared on 300 copper mesh holey carbon grids (Agar Scientific) by drop-casting dilute carbon dispersion onto a grid supported by filter paper and drying under vacuum. Raman spectra were collected on a Renishaw inVia Reflex spectrometer (1000-3000 cm⁻¹) using a 633 nm laser. Measurements of 5 areas per sample were collected and averaged. The average in-plane distances, L_a, were determined from the intensity ratio of the D- and G-bands.³⁶ Small/wide angle X-ray scattering (SAXS/WAXS) was measured on a Xenocs nano-InXider with a Cu Ka source and a two-detector setup for combined SAXS/WAXS measurements. Powder samples were packed in 2 mm Kapton capillaries and measured for 10 min. The empty capillary was measured separately and used for background subtraction. Neutron total scattering was carried out at the NIMROD⁴⁵ instrument at ISIS (Harwell, UK). Each sample was measured for 2 hours and data corrections and reduction were performed using Gudrun.⁴⁶ The N₂ and CO₂ adsorption isotherms were

obtained at 77 K and 273 K, respectively, using a Quantachrome NOVA 4200 or Autosorb iQ-C instrument. The specific surface areas were calculated with the multipoint Brunauer-Emmett-Teller (BET) method for N₂ or Dubinin-Radushkevich method for CO₂, and pore size distributions (PSD) were obtained using a non-local density functional theory (NLDFT) model from the adsorption line of the isotherm.

Electrochemical characterisation. Electrodes were prepared from slurries of 90 wt% hard carbon and 10 wt% sodium carboxymethyl cellulose binder ($M_w \sim 250,000$, Sigma Aldrich) in water, applied in a 250 µm layer on Al foil (conductive carbon coated, 18 µm, MTI corporation). The foils were cut to size (13 mm diameter) and dried under vacuum at 80 °C overnight, before being placed in the glovebox for final assembly. The electrolyte and cell preparation were conducted in an argon-filled glovebox with H₂O < 0.5 ppm, O₂ < 0.5 ppm. Sodium hexafluorophosphate (NaPF₆, Alfa Aesar, ≥99%) was first dried at 80 °C under vacuum for 16 h. A 1:1 mixture, by volume, of ethylene carbonate (EC, anhydrous 99%, Sigma Aldrich) and dimethyl carbonate (DMC, anhydrous ≥99%, Sigma Aldrich) was dried over 4 Å molecular sieves (20 vol%) for one day before use, and the solvent extracted from the top fraction to avoid contamination. A 1 M electrolyte solution was prepared by stirring NaPF₆ in EC/DMC until fully dissolved. To assemble the cell, a carbon anode, glass fibre separator (Whatman GF/B glass microfibre, 18 mm diameter) saturated with electrolyte (150 μ L), and sodium metal sheet (sodium ingot, 99.8%) metals basis, Alfa Aesar) were assembled in a CR2032 coin cell. Galvanostatic charge/discharge profiles and rate capability were measured on a BaSyTec CTS battery testing system in the potential window 0-2.5 V vs Na⁺/Na, at current densities from 30 to 600 mA g⁻¹ (0.1-2C). Cyclic voltammetry was performed on a Biologic VSP-300 potentiostat at a scan rate of 0.1 mV s⁻¹.

Solid-state nuclear magnetic resonance (NMR) spectroscopy. The cells were cycled on a Lanhe battery cycler at a rate of 0.05C until the lower cutoff voltage of 5 mV was reached. The cells were then disassembled in an argon atmosphere and the carbon electrodes were rinsed with DMC and dried under vacuum. The carbon films were separated from the aluminium current collectors, ground in a mortar and pestle, and packed into 1.3 mm outer diameter zirconia rotors. ²³Na solid-state NMR experiments were conducted on a Bruker Avance III console equipped with a 16.4 T magnet (corresponding to

Larmor frequencies of $v_0(^1\text{H}) = 700 \text{ MHz}$, $v_0(^{23}\text{Na}) = 185.3 \text{ MHz}$). A Bruker 1.3 mm double channel magic-angle spinning (MAS) probe was used with a spinning frequency of 60 kHz. Due to the short transverse relaxation time constants (T_2) of the quasi-metallic Na environments, a Bloch decay pulse sequence was used with an optimized 90° pulse length of 0.95 µs, a 50 ms recycle delay, and 40912 transients were collected for a total experimental time of 55 minutes. Spectra were obtained with the application of 1500 Hz of exponential apodization, zero filling, followed by Fourier transformation. ²³Na chemical shifts were calibrated using solid NaCl as an external secondary reference (7.21 ppm relative to 1 M NaCl(aq) at 0.0 ppm).

Density functional theory (DFT) calculations. To form an atomic scale insight into sodium storage in hard carbon motifs, six different carbon models were prepared: pristine graphitic bilayer (simulating the intercalation of sodium in graphitic stacks), graphitic bilayer with an oxygen defect, pristine graphene surface (adsorption of sodium on the hard carbon basal plane), and three oxygen-containing graphene surfaces (adsorption of sodium on defect sites on the hard carbon basal plane). Oxygen defects were chosen based on data from XPS measurements. Schematics of the computational models are included in the supporting information (Figure S8). The effect of increasing sodium concentration in the graphitic bilayer model has previously been characterised.⁴² For these atomic scale simulations, spin-polarised density functional theory (DFT) calculations as implemented in the Vienna Ab initio Simulation Package (VASP, version 5.3.5)^{47, 48, 49, 50, 51} were employed. To model the ion-electron interaction the projector-augmented wave method (PAW) was utilized,⁵² and the plane wave cut-off (800 eV) and k-space integrals (9×9×1 and 5×5×2 Γ-centred Monkhorst-Pack grid, for the surface and bulk models, respectively) were chosen so that the total energy was converged to 1 meV/atom.⁵³ The exchange-correlation energy (electronic convergence criteria of 10⁻⁵ eV and ionic convergence criteria of 10⁻³ eV·Å⁻¹) was described by the generalised gradient approximation (GGA) with the Perdew-Burke-Ernzerhof (PBE)^{54, 55} functional. Dispersion corrections (DFT-D3 method with Becke-Johnson damping) were included in all calculations to account for the polarisability of the graphitic structures and the metals.^{56, 57, 58, 59, 60} To model sodium intercalation in graphitic layers, a 4×4×2 supercell (64 atoms) was used, and for the sodium adsorption at a basal plane, or surface, a graphene monolayer

containing 72 atoms and a vacuum gap between monolayers of 15 Å was employed. These models have previously been used to study sodium adsorption and migration at defect sites,⁴⁴ and to study sodium intercalation and migration as a function of interlayer distance.^{42, 43} The sodium binding energy, E_b , was calculated according to Equation 1:⁶¹

$$E_b = \frac{E_{Bulk+xNa} - E_{Bulk} - x_{Na}E_{Na}}{x_{Na}} \tag{1}$$

where, $E_{Bulk+xNa}$ is the total energy of the systems with x_{Na} added Na, E_{Bulk} is the total energy of the systems without Na, x_{Na} is the number of added Na, and E_{Na} is the total energy of one ionic sodium. A positive E_b would mean that intercalation or storage is energetically unfavourable. The simulated sodium binding energies as a function of sodium concentration for both graphitic layers, defective graphitic layer, surface defects, and pristine surface are presented in the supporting information (Figure S9). The first added Na to the carbonaceous models with defects adsorbs or binds over the defect sites, whereas the consecutively added Na binds firstly in the vicinity of the Na at the defect site, and then further away.

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Author contributions

H.Au designed the study and drafted the article. H.Au and H.Al. synthesised the hard carbon samples and conducted the electrochemical testing for the NIB cells. H.Au obtained the SEM, XPS, TEM and Raman data. H.Au and H.Al. conducted the gas adsorption experiments. A.C.S.J. conducted the SAXS/WAXS measurements and analysis. A.C.S.J. and T.F.H. performed the SANS/WANS measurements and analysis. E.O. performed the DFT simulations and analysis. C.A.O. and T.S. performed the NMR measurements. H.Al., A.C.S.J., E.O., C.A.O. revised and edited the manuscript. C.P.G., Q.C., A.J.D. and M.-M.T. provided supervision and funding, and revised and edited the final manuscript.

Competing interests

The authors declare no competing interests.